

- Check Understanding** 1 Graph each set of points. Which model is most appropriate for each set?
- a.  $(-1.5, -2), (0, 2), (1, 4), (2, 6)$
- b.  $(-1, 1), (0, 0), (1, 1), (2, 4)$
- c.  $(-1, 0.5), (0, 1), (1, 2), (2, 4)$

You can also analyze data numerically to find the best model.

In Lesson 5-6, you learned that the terms of an arithmetic sequence have a common difference. You can model an arithmetic sequence with a linear function.

	x	y	
	-2	-2	
+ 1	-1	2	+ 4
+ 1	0	6	+ 4
+ 1	1	10	+ 4
+ 1	2	14	+ 4

The y-coordinates have a common difference of 4. A linear model fits the data.

In Lesson 8-6, you learned that the terms of a geometric sequence have a common ratio. You can model a geometric sequence with an exponential function.

	x	y	
	-2	$\frac{1}{9}$	
+ 1	-1	$\frac{1}{3}$	$\times 3$
+ 1	0	1	$\times 3$
+ 1	1	3	$\times 3$
+ 1	2	9	$\times 3$

The y-coordinates have a common ratio of 3. An exponential model fits the data.

Data from quadratic functions show a different pattern. For linear data, the first differences are the same. For quadratic data, the second differences are the same. If data have a common second difference, then you can model them with a quadratic function.

	x	y		
	-1	16		
+ 1	0	2	- 14	
+ 1	1	-2	- 4	+ 10
+ 1	2	4	+ 6	+ 10
+ 1	3	20	+ 16	+ 10
+ 1	4	46	+ 26	+ 10

↑ first difference      ↑ second difference

The y-coordinates have a common second difference of 10. A quadratic model fits the data.